


Day 46 Warm-Up:

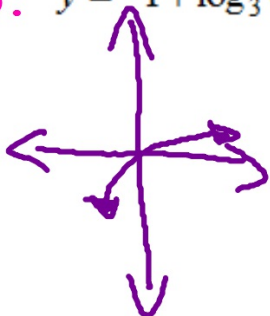
Sketch the following then state the domain (and range)

1. $y = 2^{x+3} - 1$




d: $(-\infty, \infty)$
r: $(-1, \infty)$

3. $y = -1 + \log_3(x+2)$



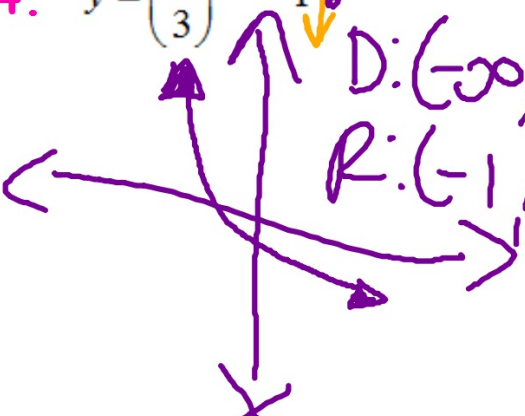
D: $(-2, \infty)$
R: ~~$(-1, \infty)$~~
 $(-\infty, \infty)$

2. $y = \log_2(x+3) - 2$



~~$R: (-2, \infty)$~~
D: $(-3, \infty)$

4. $y = \left(\frac{1}{3}\right)^{x-1} - 1$



D: $(-\infty, \infty)$
R: $(-1, \infty)$

$$1. \frac{4}{x} + \frac{1}{x^2} = \frac{1}{5x^2} \quad \left\{ -\frac{1}{5} \right\}$$

$$2. \frac{x-5}{x^2} + \frac{1}{x} = \frac{6}{x} \quad \left\{ -\frac{5}{4} \right\}$$

$$3. \frac{4}{n+1} + \frac{1}{n^2-5n-6} = \frac{1}{n-6} \quad \{8\}$$

$$4. \frac{5}{p+6} - \frac{1}{p^2+6p} = \frac{2}{p^2+6p} \quad \left\{ \frac{3}{5} \right\} = -6$$

$$5. \frac{5}{(x+1)} = \frac{6}{(x^2-2x-3)} + \frac{1}{(x-3)} \quad \left\{ \frac{11}{2} \right\}$$

$$6. \frac{k+1}{k} = 1 - \frac{k^2-3k-4}{4k} \quad \{3\}$$

Checking with
two different
methods

zoom box

$(5/(p+6)) - (1/(p^2+6p))$
2nd term (cancel)
5: intersect

Given $f(x) = \frac{g(x)}{h(x)}$

Factor $g(x)$ and $h(x)$, then cancel common factors.

Vertical Asymptotes

Set the denominator = 0 and solve for x .

Holes (point discontinuity)

Set cancelled factors = 0 and solve for x . Substitute x into the simplified expression to find y . Write the answer as an ordered pair.

Horizontal Asymptotes

$f(x) = \frac{\text{smaller degree}}{\text{larger degree}} \frac{x^2}{x^3}$

$y = 0$

$f(x) = \frac{\text{same degree}}{\text{same degree}} \frac{2x^4}{3x^4}$

$y = \frac{\text{lead coefficient of numerator}}{\text{lead coefficient of denominator}}$

$f(x) = \frac{\text{larger degree}}{\text{smaller degree}} \frac{x^6}{x^3}$

none

$\frac{1}{2} = .5 \quad \frac{1}{10} = .1 \quad \frac{1}{152} = .0066$

$\frac{1}{1287} = .000777$

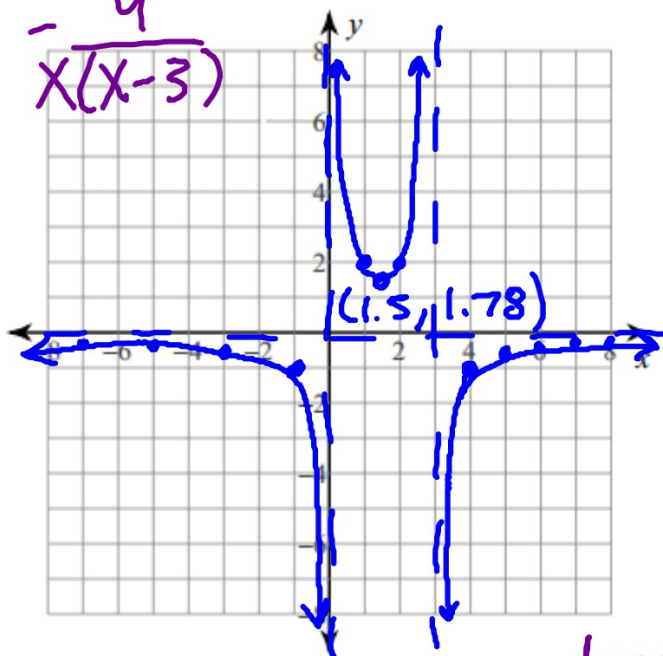
$\frac{2}{1} = 2 \quad \frac{10}{1} = 10 \quad \frac{152}{1} = 152 \quad \frac{3873}{8}$



$$f(x) = -\frac{4}{x^2 - 3x}$$

$$-\frac{4}{x(x-3)}$$

① Factor & Simplify



Domain: $(-\infty, 0) \cup (0, 3) \cup (3, \infty)$

Range: $(-\infty, 0) \cup [1.78, \infty)$

Holes: $\frac{0}{0}$ (nothing cancelled)

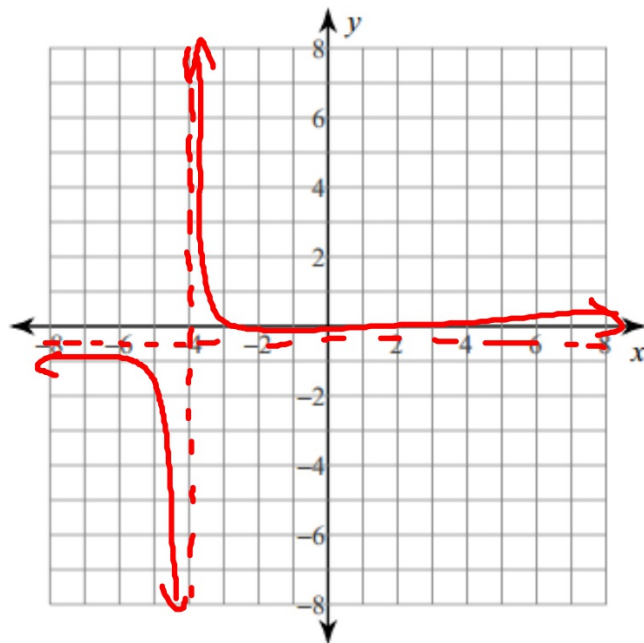
VA: $x=0$ & 3 $x(x-3)=0$

HA: $y=0$ $x=0$ $x-3=0$

degrees $\frac{0}{2}$ $\frac{L}{H}$

x

$$f(x) = \frac{x - 4}{-4x - 16}$$



Domain: $(-\infty, -4) \cup (-4, \infty)$

Range: $(-\infty, 1/4) \cup (1/4, \infty)$

Holes: none

VA: $x = -4$

HA: $y = \frac{1}{4}$